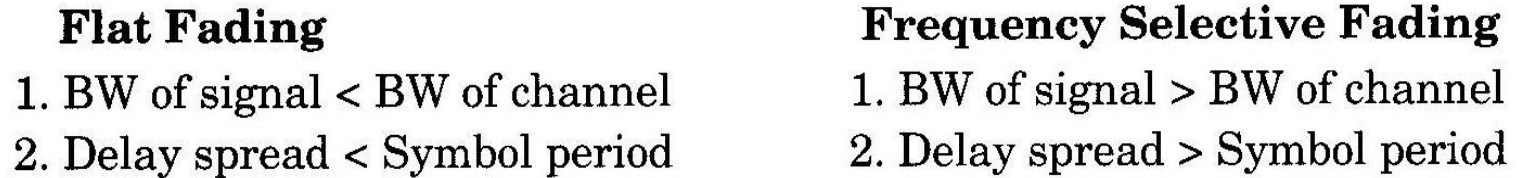


# Unit-1

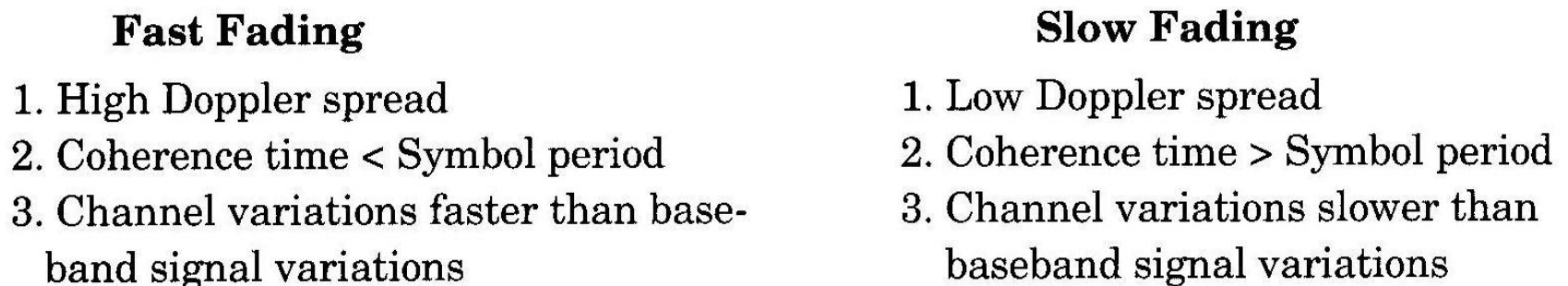
## **Small-Scale Fading**

(Based on multipath time delay spread)



## **Small-Scale Fading**

(Based on Doppler spread)

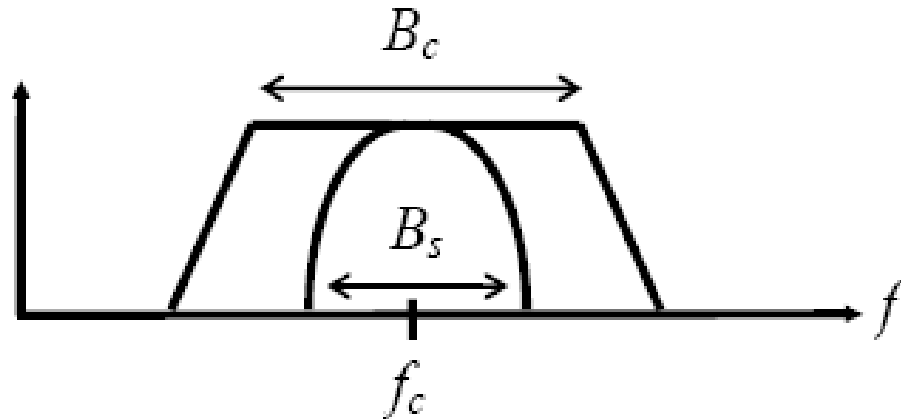


**Figure 5.11** Types of small-scale fading.

## 1) Fading due to Multipath Delay

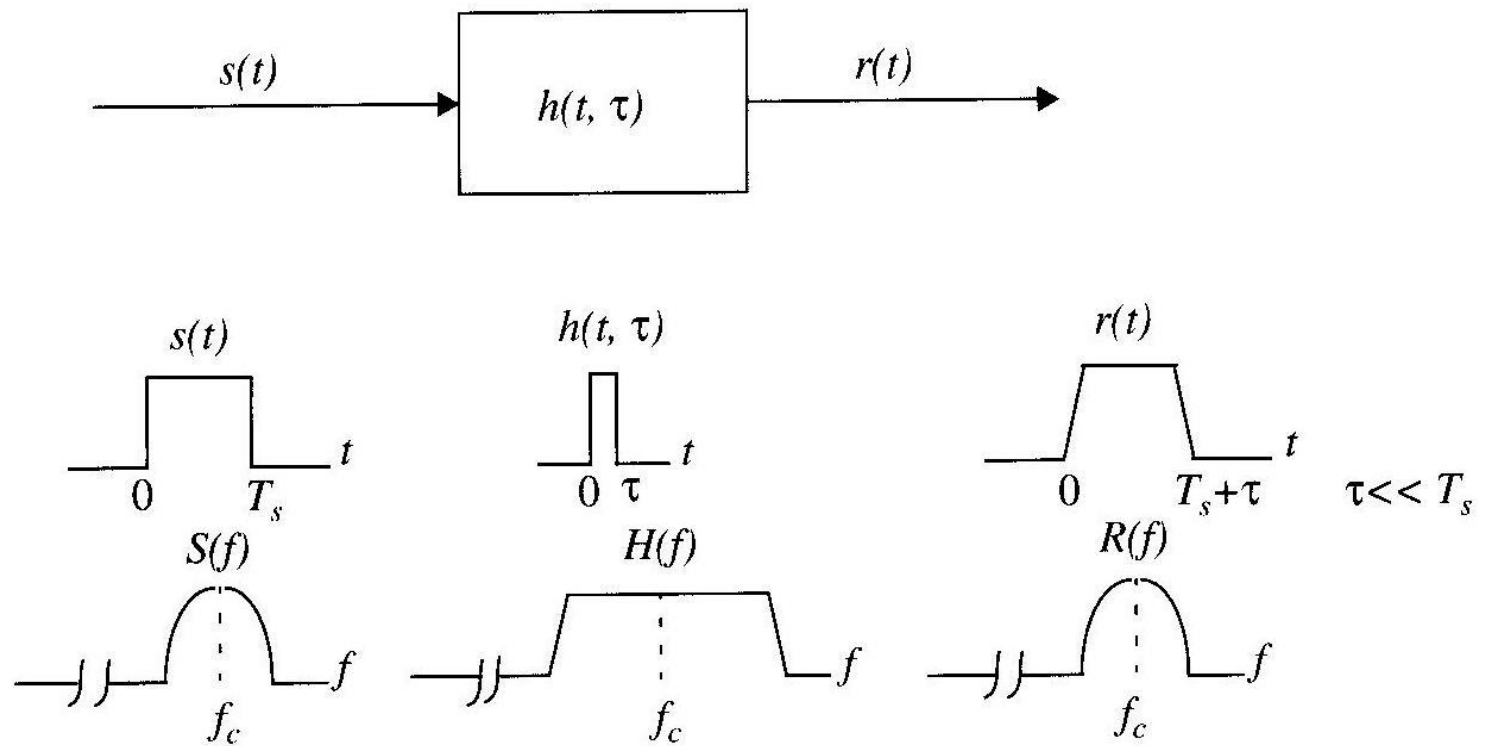
A) Flat Fading  $\rightarrow B_s \ll B_c$  or  $T_s \gg \sigma_\tau$

- $T_s \geq 10\sigma_\tau$
- signal fits easily within the bandwidth of the channel
- channel BW  $\gg$  signal BW



- most commonly occurring type of fading

- spectral properties of Tx signal are preserved
  - signal is called a *narrowband* channel, since the bandwidth of the signal is narrow with respect to the channel bandwidth
  - signal is not distorted
- What does  $T_s \gg \sigma_\tau$  mean??
  - all multipath signals arrive at mobile Rx during 1 symbol period
  - ∴ Little intersymbol interference occurs (no multipath components arrive late to interfere with the next symbol)

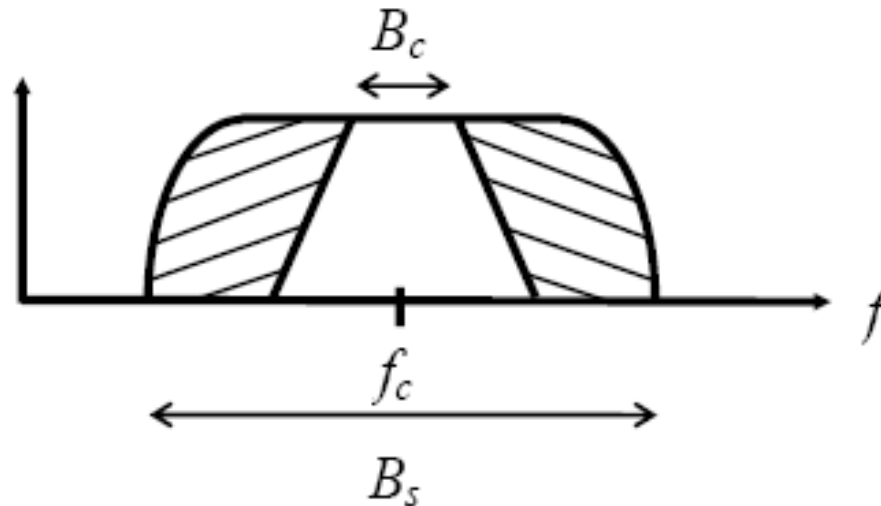


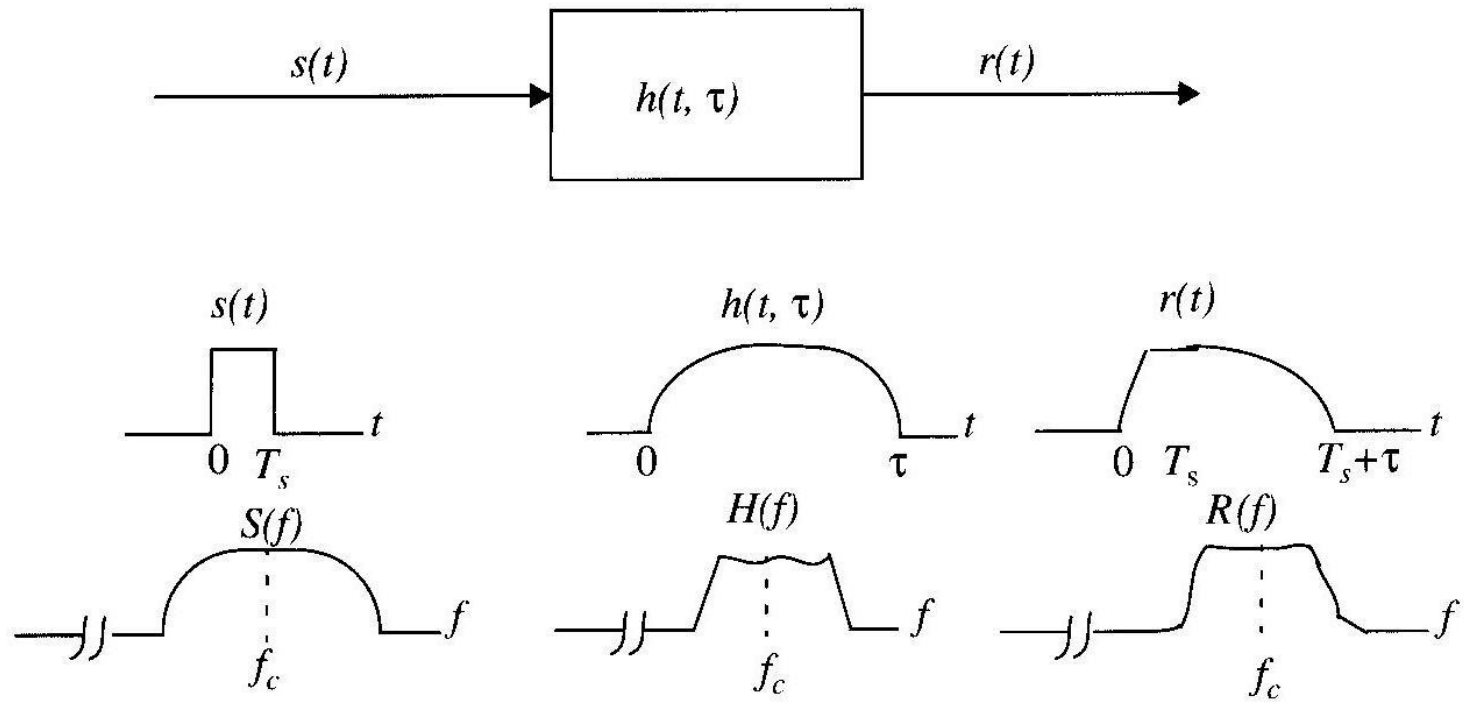
**Figure 5.12** Flat fading channel characteristics.

- flat fading is generally considered **desirable**
  - Even though fading in amplitude occurs, the signal is not distorted
  - Forward link → can increase mobile Rx gain (automatic gain control)
  - Reverse link → can increase mobile Tx power (power control)
  - Can use diversity techniques (described in a later lecture)

B) Frequency Selective Fading  $\rightarrow B_s > B_c$  or  $T_s < \sigma_\tau$

- $T_s \leq 10\sigma_\tau$
- $B_s > B_c \rightarrow$  certain frequency components of the signal are attenuated much more than others





**Figure 5.13** Frequency selective fading channel characteristics.



- $T_s < \sigma_\tau \rightarrow$  delayed versions of Tx signal arrive during **different** symbol periods
  - e.g. receiving an LOS  $\rightarrow$  “1” & multipath “0” (from prior symbol!)
  - This results in intersymbol interference (ISI)
  - Undesirable
- it is very difficult to predict mobile Rx performance with frequency selective channels

- But for high bandwidth applications, channels with likely be frequency selective
  - a new modulation approach has been developed to combat this.
  - Called **OFDM**
- One aspect of OFDM is that it separates a wideband signal into many smaller narrowband signals
  - Then adaptively adjusts the power of each narrowband signal to fit the characteristics of the channel at that frequency.
  - Results in much improvement over other wideband transmission approaches (like CDMA).

- OFDM is used in the new 802.11g 54 Mbps standard for WLAN's in the 2.4 GHz band.
- Previously it was thought 54 Mbps could only be obtained at 5.8 GHz using CDMA, but 5.8 GHz signals attenuate much more quickly.
- Signals are split using signal  $\rightarrow$  FFT, break into pieces in the frequency domain, use inverse FFT to create individual signals from each piece, then transmit.

## 2) Fading due to Doppler Spread

- Caused by motion of Tx and Rx and reflection sources.

**A) Fast Fading**  $\rightarrow B_s < B_D$  or  $T_s > T_c$

- $B_s < B_D$

- Doppler shifts significantly alter spectral BW of TX signal
- signal “spreading”

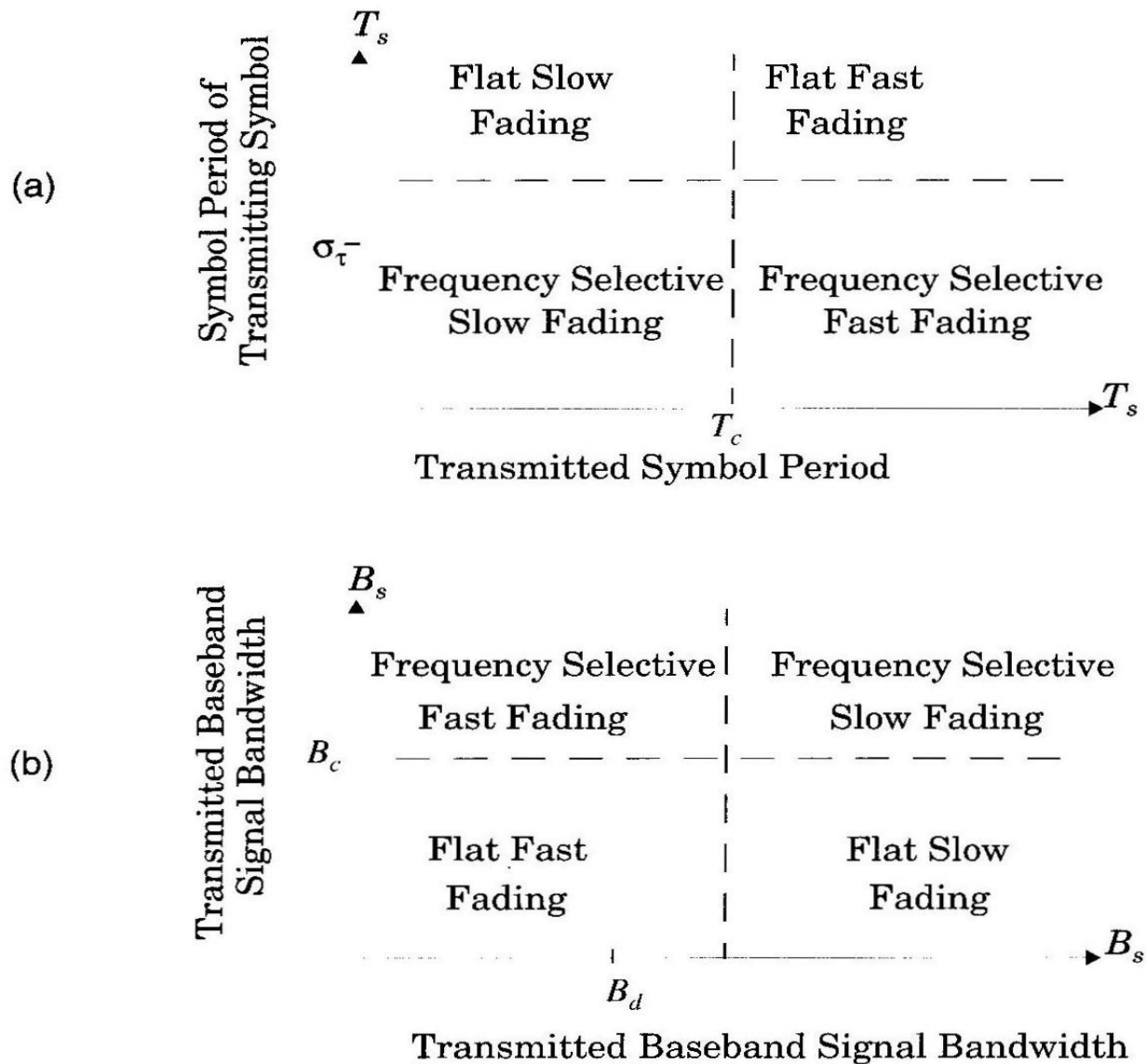
- $T_s > T_c$

- MRC changes within 1 symbol period
- rapid amplitude fluctuations

- uncommon in most digital communication systems

## B) Slow Fading $\rightarrow T_s \ll T_c$ or $B_s \gg B_D$

- MRC constant over many symbol periods
- slow amplitude fluctuations
- for  $v = 60$  mph @  $f_c = 2$  GHz  $\rightarrow B_D = 178$  Hz
  - $\therefore B_s \approx 2$  kHz  $\gg B_D$ 
    - $B_s$  almost always  $\gg B_D$  for most applications
- \*\* NOTE: Typically use a factor of 10 to designate “ $\gg$ ” \*\*



**Figure 5.14** Matrix illustrating type of fading experienced by a signal as a function of: (a) symbol period; and (b) baseband signal bandwidth.

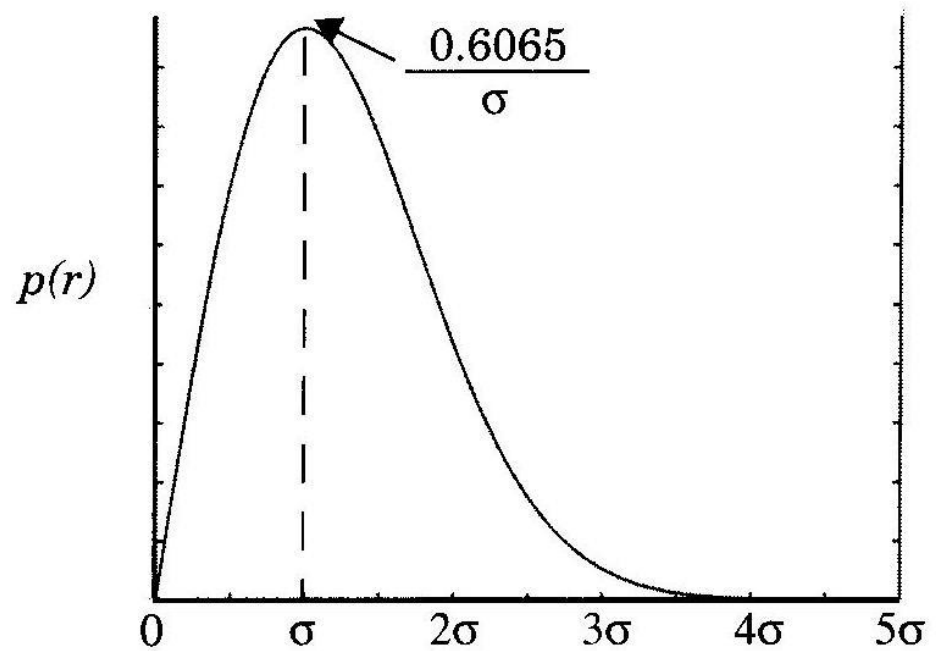
## VI. Fading Signal Distributions

- Rayleigh probability distribution function →

$$P(r) = \frac{r}{\sigma^2} \exp\left(-\frac{r^2}{2\sigma^2}\right) \quad 0 \leq r \leq \infty$$

- Used for flat fading signals.
- Formed from the sum of two Gaussian noise signals.
- $\sigma$  : RMS value of Rx signal **before** detection (demodulation)
- common model for Rx signal variation
  - urban areas → heavy clutter → no LOS path
- probability that signal does not exceeds predefined threshold level  $R$

$$P(R) = Pr(r \leq R) = \int_0^R p(r) dr = 1 - \exp\left(-\frac{R^2}{2\sigma^2}\right)$$



Received signal envelope voltage  $r$  (volts)

**Figure 5.16** Rayleigh probability density function (pdf).



- $r_{mean}$  : The mean value of Rayleigh distribution

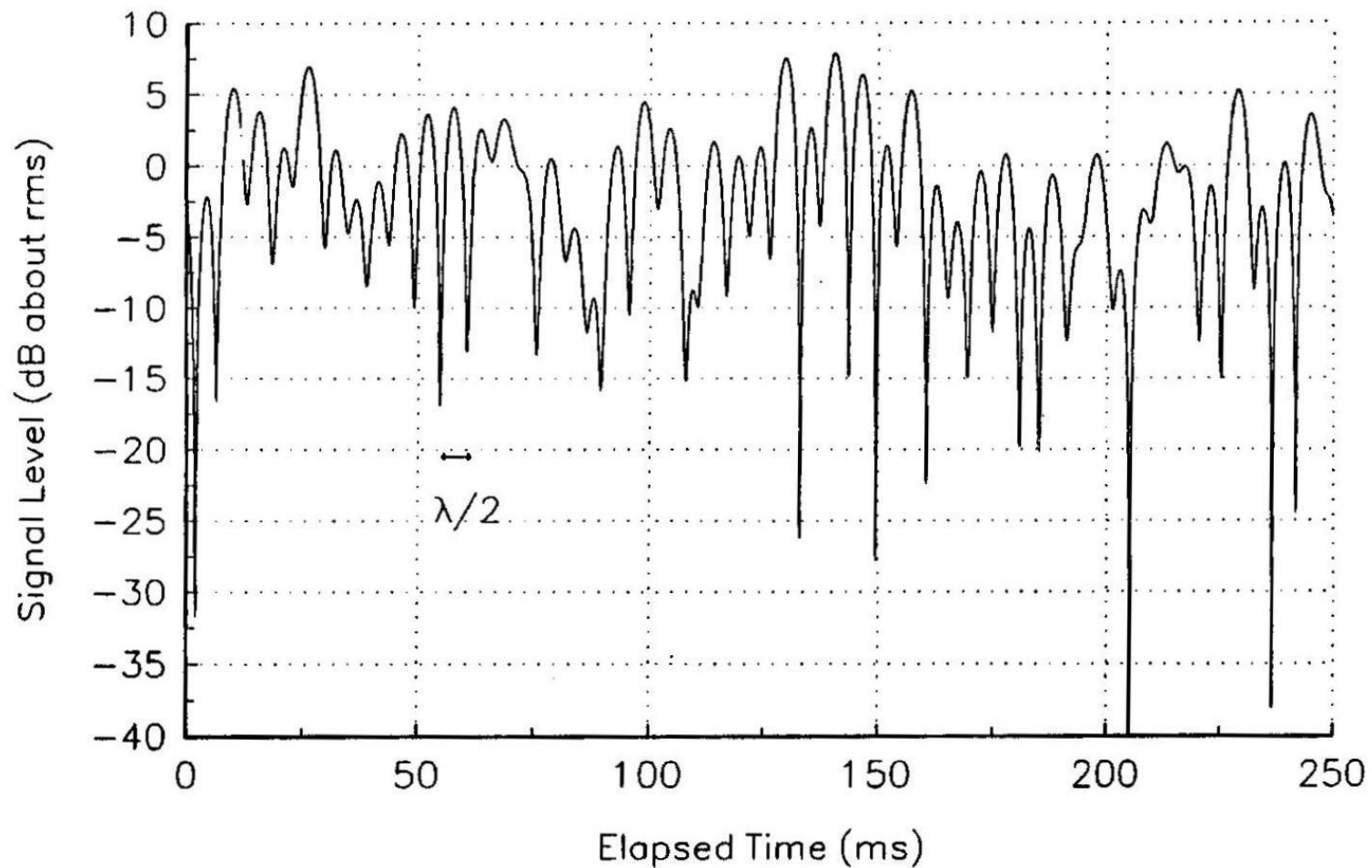
$$r_{mean} = E[r] = \int_0^{\infty} r p(r) dr = \sigma \sqrt{\frac{\pi}{2}} = 1.2533\sigma$$

- $\sigma_r^2$  : The variance of Rayleigh distribution; ac power of signal envelope

$$\begin{aligned}\sigma_r^2 &= E[r^2] - E^2[r] = \int_0^{\infty} r^2 p(r) dr - \frac{\sigma^2 \pi}{2} \\ &= \sigma^2 \left( 2 - \frac{\pi}{2} \right) = 0.4292\sigma^2\end{aligned}$$

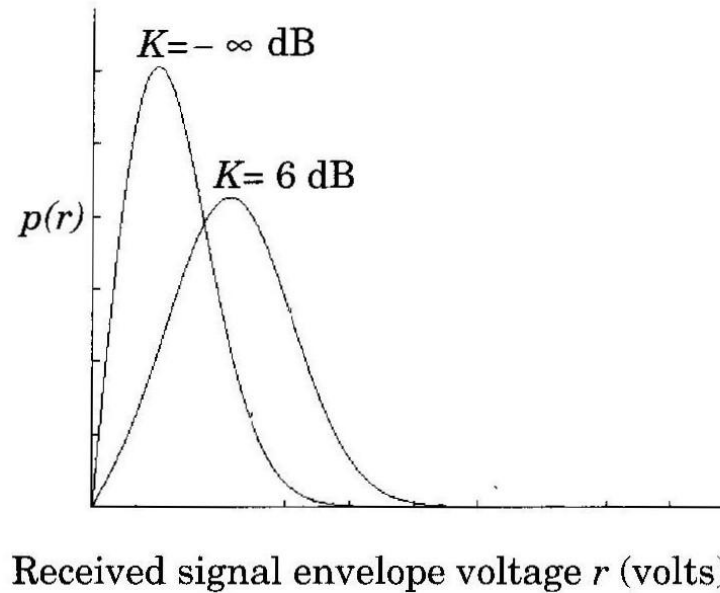
- $\sigma$  : RMS value of Rx signal **before** detection (demodulation)

Typical simulated Rayleigh fading at the carrier  
Receiver speed = 120 km/hr



**Figure 5.15** A typical Rayleigh fading envelope at 500 MHz [from [Fun93] © IEEE].

- Ricean Probability Distribution Function
    - one dominant signal component along with weaker multipath signals
    - dominant signal  $\rightarrow$  LOS path
      - suburban or rural areas with light clutter
    - becomes Rayleigh distribution if no dominant component
- $$p(r) = \begin{cases} \frac{r}{\sigma^2} e^{-\frac{(r^2 + A^2)}{2\sigma^2}} I_0\left(\frac{Ar}{\sigma^2}\right) & \text{for } (A \geq 0, r \geq 0) \\ 0 & \text{for } (r < 0) \end{cases}$$



**Figure 5.18** Probability density function of Ricean distributions:  $K = -\infty$  dB (Rayleigh) and  $K = 6$  dB. For  $K \gg 1$ , the Ricean pdf is approximately Gaussian about the mean.